

# Grid WAR+

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## Adjusting for opposing offensive quality

Suppose we knew  $p_i$ , the probability that batting team  $i$  with a randomly drawn defense defeats a randomly drawn opposing team. For an average offensive team,  $p_i = 1/2$ . Then

$$dp_i := p_i - 1/2 \tag{0.1}$$

is offense  $i$ 's win probability above that of an average offense. Then a starting pitcher's Grid WAR in a game, adjusted for the offensive quality of the opposing team  $i$  is

$$\text{GWAR+} := \text{GWAR} + dp_i \times \frac{I}{9}, \tag{0.2}$$

where  $I$  is the starter's number of innings pitched in that game. The better the opposing offensive team, the more WAR credited to the starter.

We need to estimate  $\{p_i\}$ . To do so, suppose we knew  $\mu_i$ , the mean runs scored in a game by team  $i$  against a randomly drawn defense. Given  $\mu_i$ , we model

$$p_i = \frac{1}{29} \sum_{j \neq i} \left\{ \mathbb{P}(\text{Poisson}(\mu_i) > \text{Poisson}(\mu_j)) + \frac{1}{2} \mathbb{P}(\text{Poisson}(\mu_i) = \text{Poisson}(\mu_j)) \right\}, \tag{0.3}$$

which is explicitly computable using the Skellam distribution. To estimate  $\{\mu_i\}$ , we use ridge regression. Our dataset consists of all half-innings in a given season, each datapoint (row)  $j$  represents a half-inning, the response column  $y_j$  is the actual runs scored in that half inning, we use the park factor  $\hat{\alpha}$  as an offset term (estimated previously), and we use fixed effects for the offense and defensive team. We tune the ridge parameter  $\lambda$  using cross validation.